Objective & Strategy	Concrete	Pictorial	Abstract
ivision as sharing se Gordon ITPs for nodelling	66	Children use pictures or shapes to share quantities.	12 shared between 3 is 4
		Sharing:	
	10	12 shared between 3 is 4	
	ve 10 cubes, can you share them equally in oups?		

Objective & Strategy	Concrete	Pictorial	Abstract
Division as sharing	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities.  8 + 2 = 4  Children use bar modelling to show and support understanding.	12 ÷ 3 = 4
Division as grouping	Divide quantities into equal groups.  Use cubes, counters, objects or place value counters to aid understanding.	Use number lines for grouping  12 ÷ 3 = 4  Think of the par as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.  20 ÷ 5 = ? 5 x ? = 20	28 ÷ 7 = 4  Divide 28 into 7 groups. How many are in each group?

Objective &	Concrete	Pictorial	Abstract
Strategy  Division as grouping	Use cubes, counters, objects or place value counters to aid understanding.  24 divided into groups of $6 = 4$ 96 ÷ 3 = 32	Continue to use bar modelling to aid solving division problems. $ 20 $ $ ? $ $ 20 \div 5 = ? $ $ 5 \times ? = 20 $	How many groups of 6 in 24? 24 ÷ 6 = 4
Division with arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created.  Eg 15 ÷ 3 = 5 5 x 3 = 15  15 ÷ 5 = 3 3 x 5 = 15	Draw an array and use lines to split the array into groups to make multiplication and division sentences	Find the inverse of multiplication and division sentences by creating eight linking number sentences.  7 x 4 = 28  4 x 7 = 28  28 ÷ 7 = 4  28 ÷ 4 = 7  28 = 7 x 4  28 = 4 x 7  4 = 28 ÷ 7  7 = 28 ÷ 4

Objective &	Concrete	Pictorial	Abstract
Divide at least 3 digit numbers by 1 digit. Short Division	96 ÷ 3  Tens Units  3  2  3  3  42 ÷ 3=  Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.	Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.  Encourage them to move towards counting in multiples to divide more efficiently.	Begin with divisions that divide equally with no remainder.  2 1 8 3 4 8 7 2  Move onto divisions with a remainder.  8 6 r 2 3 5 4 3 2  Finally move into decimal places to divide the total accurately.  1 4 6 16 21 3 5 5 1 1 0

Y4-6

E

Step 1-a remainder in the ones

- 4 does not go into 1 (hundred). So combine the 1 hundred with the 6 tens (160).
- 4 goes into 16 four times.
- 4 goes into 5 once, leaving a remainder of 1.

- 8 does not go into 3 of the thousands. So combine the 3 thousands with the 2 hundreds (3,200).
- 8 goes into 32 four times  $(3,200 \div 8 = 400)$
- 8 goes into 0 zero times (tens).
- 8 goes into 7 zero times, and leaves a remainder of 7.

Step 1 continued...

When dividing the ones, 4 goes into 7 one time. Multiply  $1 \times 4 = 4$ , write that four under the 7, and subract. This finds us the remainder of 3.

Check:  $4 \times 61 + 3 = 247$ 

When dividing the ones, 4 goes into 9 two times. Multiply  $2 \times 4 = 8$ , write that eight under the 9, and subract. This finds us the remainder of 1.

Check:  $4 \times 402 + 1 = 1,609$ 

Step 2—a remainder in the tens

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
t o 2 2 )5 8	2 2)58 -4 1	t o 29 2)5 <mark>8</mark> -4   18
Two goes into 5 two times, or 5 tens    2 = 2 whole tens but there is a remainder!	To find it, multiply 2 × 2 = 4, write that 4 under the five, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
2 9 2 ) 5 8 -4 1 8	2 9 2 ) 5 8 -4 1 8 -1 8	2 9 2 ) 5 8 -4 1 8 -1 8
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract.	The division is over since there are no more digits in the dividend. The quotient is 29.

Step 2—a remainder in any of the place values

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
1 2)278	2)278 =20	18 2)278 -2↓ 07
Two goes into 2 one time, or 2 hundreds + 2 = 1 hundred.	Multiply 1 × 2 = 2, write that 2 under the two, and subtract to find the remainder of zero.	Next, drop down the 7 of the tens next to the zero.
Divide.	Multiply & subtract.	Drop down the next digit.
1 3 2 ) 2 7 8 -2 0 7	13 2)278 -2 07 -6	13 2)278 -2 07 -6 18
Divide 2 into 7. Place 3 into the quotient.	Multiply 3 × 2 = 6, write that 6 under the 7, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the 1 leftover ten.
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
13 <mark>9</mark> 2)278 -2 07 -6 18	139 2)278 -2 07 -6 18 -18	2)278 -207 -6 18 -18
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract to find the remainder of zero.	There are no more digits to drop down. The quotient is 139.