Objective & Strategy	Concrete  Children continue to use dienes or py					Abstract		
Y4—add numbers with up to 4 digits	counters to a ten and te	add, exchanging on tens for a hund or a thousand.	ten ones for	• •	***	:	**	3517
	Hundreds	Tens	Ones	7 Draw represen	1	5 ing pv g	1 rid.	+ 3 9 6 3 9 1 3  Continue from previous work to carry hundreds as well as tens.  Relate to money and measures.
Y5—add numbers with more than 4 digits.  Add decimals with 2 decimal places, including money.	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	ecimal place value	e counters	2.37 + 8  Hens 00  000000000000000000000000000000000	145	000 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	hundred &s	72.8 +54.6 127.4 1 1 € 2 3 · 5 9 + € 7 · 5 5 € 3   ·   4
6—add several num- pers of increasing com- plexity	As Y5			As Y5				81,059 3668 15,301 + 20,551 120,579
Including adding money, measure and decimals with different numbers of decimal points.								2 3 · 3 6   9 · 0 8 0   5 9 · 7 7 0   1 · 3 0 0   9 3 · 5   1   2   1 · 2   1   2   1

Objective & Strategy	Concrete	Pictorial	Abstract
Subtracting tens and ones Year 4 subtract with up to 4 digits. Introduce decimal subtraction through context of money	234 - 179  O O O O O O O O O O O O O O O O O O O	Children to draw pv counters and show their exchange—see Y3	2 x 5 4 - 1 5 6 2 1 1 9 2 Use the phrase 'take and make' for exchange
Year 5- Subtract with at least 4 dig- its, including money and measures. Subtract with decimal values, including mixtures of integers and decimal and aligning the decimal	As Year 4	Children to draw pv counters and show their exchange—see Y3	*3 * X '0 *8 '6 - 2   2 8 2 8,9 2 8 Use zeros for place- holders 3 7 2 · 5, 6 7 9 6 · 5
Year 6—Subtract with increasingly large and more complex numbers and decimal values.			**************************************

Objective & Strategy	Concrete	Pictorial	Abstract	Y5.6
Column Multiplication for 3 and 4 digits x 1 digit.	Hundreds Tens Ones It is important at this stage that they always multiply the ones first.  Children can continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping. 321 x 2 = 642	× 300 20 7 4 1200 80 28	327 x 4 28 80 1200 1308  This will lead to a compact method.	
Column multiplication	Manipulatives may still be used with the corresponding long multiplication modelled alongside.	Continue to use bar modelling to support problem solving	1 8	ICATION X

Objective &	Concrete	Pictorial	Abstract
Strategy			
Multiplying decimals			Remind children that the single digit belong
p to 2 decimal plac-			in the units column. Line up the decimal
es by a single digit.			points in the question and the answer.
			3 · 1 9
			× 8 2 5 · 5 2
			25.52
			1 7

Objective &	Concrete	Pictorial	Abstract
Divide at least 3 digit numbers by 1 digit. Short Division	96 ÷ 3  Tens Units  3  2  3  3  42 ÷ 3=  Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.	Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.  Encourage them to move towards counting in multiples to divide more efficiently.	Begin with divisions that divide equally with no remainder.  2 1 8 3 4 8 7 2  Move onto divisions with a remainder.  8 6 r 2 3 5 4 3 2  Finally move into decimal places to divide the total accurately.  1 4 6 16 21 3 5 5 1 1 0

Y4-6

E

Step 1-a remainder in the ones

- 4 does not go into 1 (hundred). So combine the 1 hundred with the 6 tens (160).
- 4 goes into 16 four times.
- 4 goes into 5 once, leaving a remainder of 1.

- 8 does not go into 3 of the thousands. So combine the 3 thousands with the 2 hundreds (3,200).
- 8 goes into 32 four times  $(3,200 \div 8 = 400)$
- 8 goes into 0 zero times (tens).
- 8 goes into 7 zero times, and leaves a remainder of 7.

Step 1 continued...

When dividing the ones, 4 goes into 7 one time. Multiply  $1 \times 4 = 4$ , write that four under the 7, and subract. This finds us the remainder of 3.

Check:  $4 \times 61 + 3 = 247$ 

When dividing the ones, 4 goes into 9 two times. Multiply  $2 \times 4 = 8$ , write that eight under the 9, and subract. This finds us the remainder of 1.

Check:  $4 \times 402 + 1 = 1,609$ 

Step 2—a remainder in the tens

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.	
t o 2 2 )5 8	2 2)58 -4 1	t o 29 2)5 <mark>8</mark> -4   18	
Two goes into 5 two times, or 5 tens    2 = 2 whole tens but there is a remainder!	To find it, multiply 2 × 2 = 4, write that 4 under the five, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.	

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
2 9 2 ) 5 8 -4 1 8	2 9 2 ) 5 8 -4 1 8 -1 8	2 9 2 ) 5 8 -4 1 8 -1 8
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract.	The division is over since there are no more digits in the dividend. The quotient is 29.

Step 2—a remainder in any of the place values

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
1 2)278	2)278 =20	18 2)278 -2↓ 07
Two goes into 2 one time, or 2 hundreds + 2 = 1 hundred.	Multiply 1 × 2 = 2, write that 2 under the two, and subtract to find the remainder of zero.	Next, drop down the 7 of the tens next to the zero.
Divide.	Multiply & subtract.	Drop down the next digit.
1 3 2 ) 2 7 8 -2 0 7	13 2)278 -2 07 -6	13 2)278 -2 07 -6 18
Divide 2 into 7. Place 3 into the quotient.	Multiply 3 × 2 = 6, write that 6 under the 7, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the 1 leftover ten.
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
13 <mark>9</mark> 2)278 -2 07 -6 18	139 2)278 -2 07 -6 18 -18	2)278 -207 -6 18 -18
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract to find the remainder of zero.	There are no more digits to drop down. The quotient is 139.